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PONTIFICIA  
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VALPARAÍSO

# Black Holes and Holography

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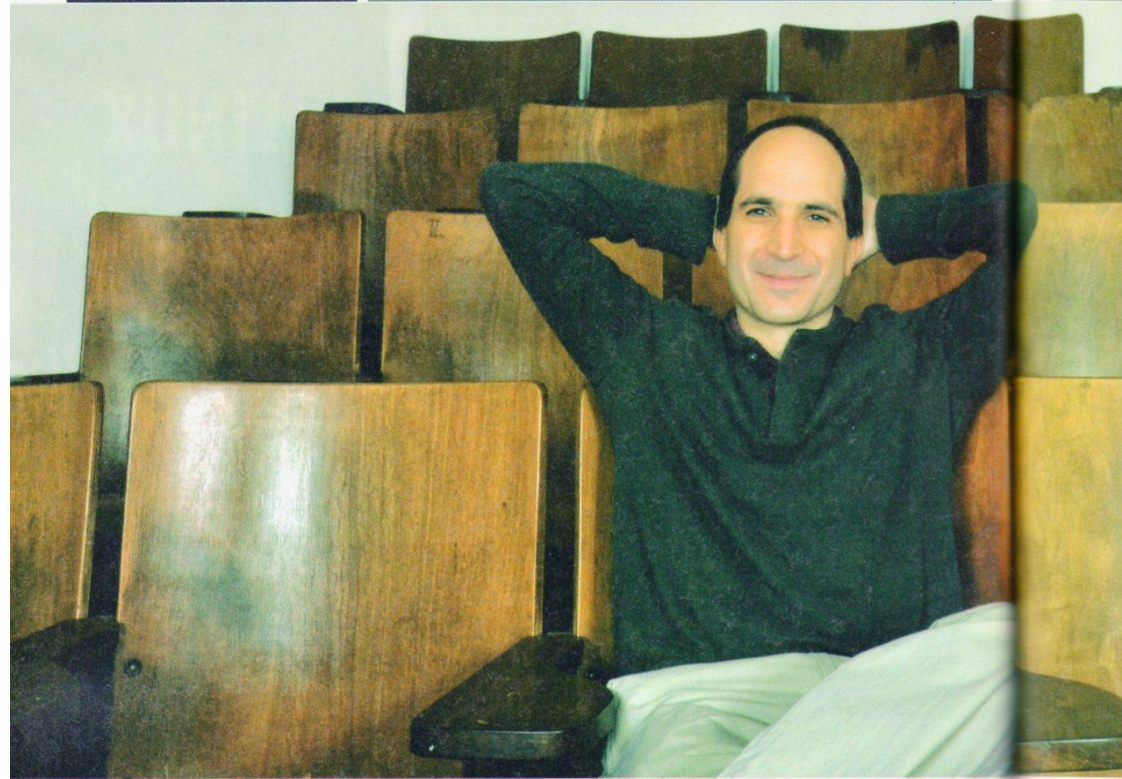


29 August 2019

Departamento de Astronomía, Universidad de Chile

# AdS/CFT correspondence

- Proposal of the Argentinean physicist Juan Maldacena 1997
- Special case of the so called Holographic principle
- In five years, the article of Maldacena had 3000 citations and it has become one of the most evident conceptual advances of theoretical physics of 90's.
- At the moment the paper has 14845 citations



## EL PODER DE LA MENTE

THE POWER OF THE MIND

El más brillante de los científicos argentinos habla sobre el origen de las ideas, la música de las matemáticas y su "viaje" a través del espacio-tiempo con lápiz y papel.  
*/ The most brilliant Argentine scientist tells us about the origins of ideas, music and mathematics, and of the "journey" through time and space that he took with pencil and paper.*

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# AdS/CFT

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Adv. Theor. Math. Phys. **2** (1998) 231–252

## The Large N Limit of Superconformal field theories and supergravity

Juan Maldacena<sup>1</sup>

Lyman Laboratory of Physics  
Harvard University  
Cambridge, MA 02138, U.S.A.

El más brillante de los científicos argentinos habla sobre el origen de las ideas, la música de las matemáticas y su “viaje” a través del espacio-tiempo con lápiz y papel.  
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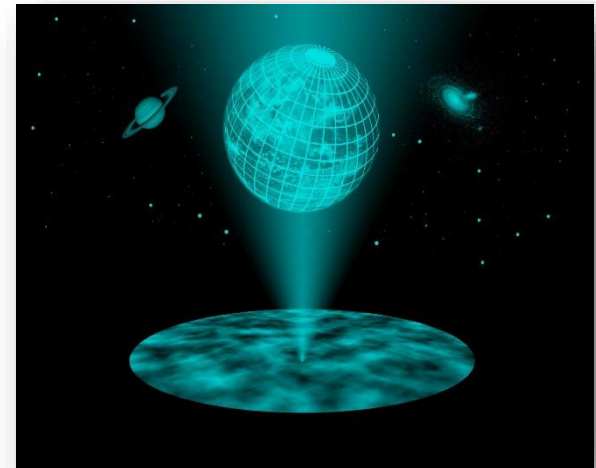
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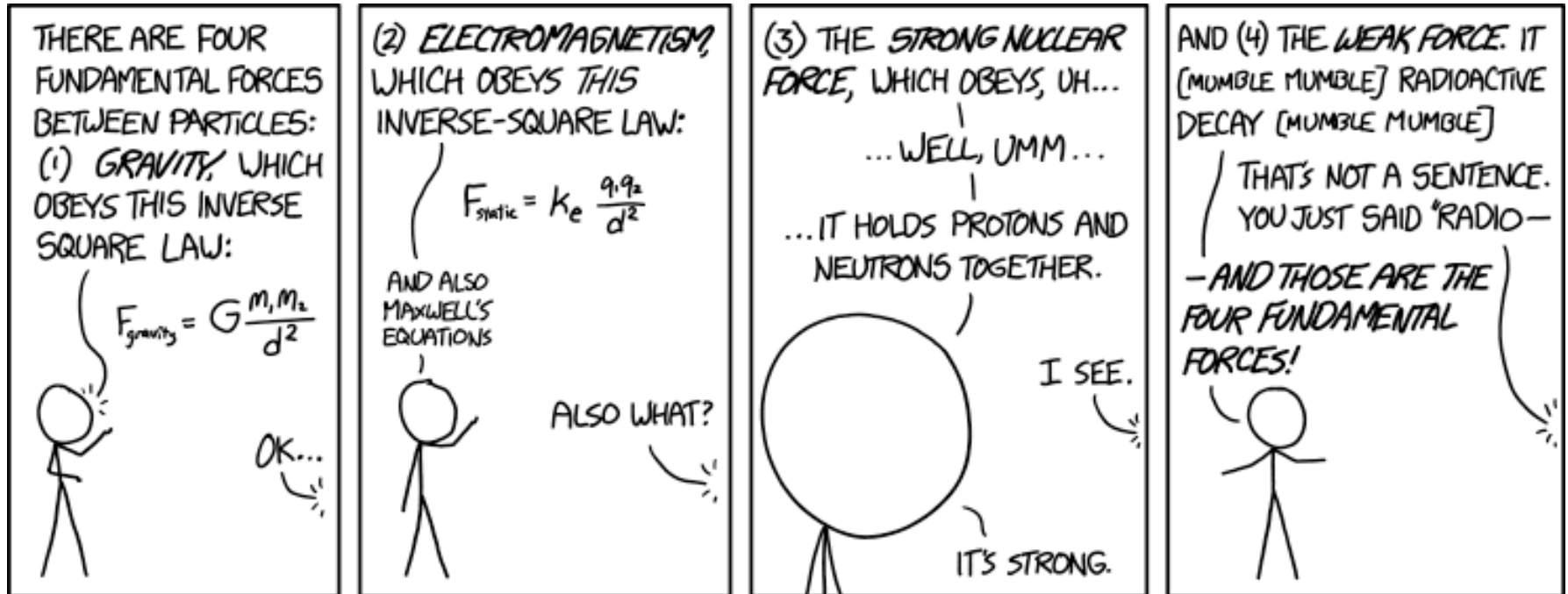
# This presentation is about...

- From where the inspiration of holography in gravity comes from
- Why this idea is so successful
- What is a holographic projection of a black hole
- Our contribution to the subject
- Challenges



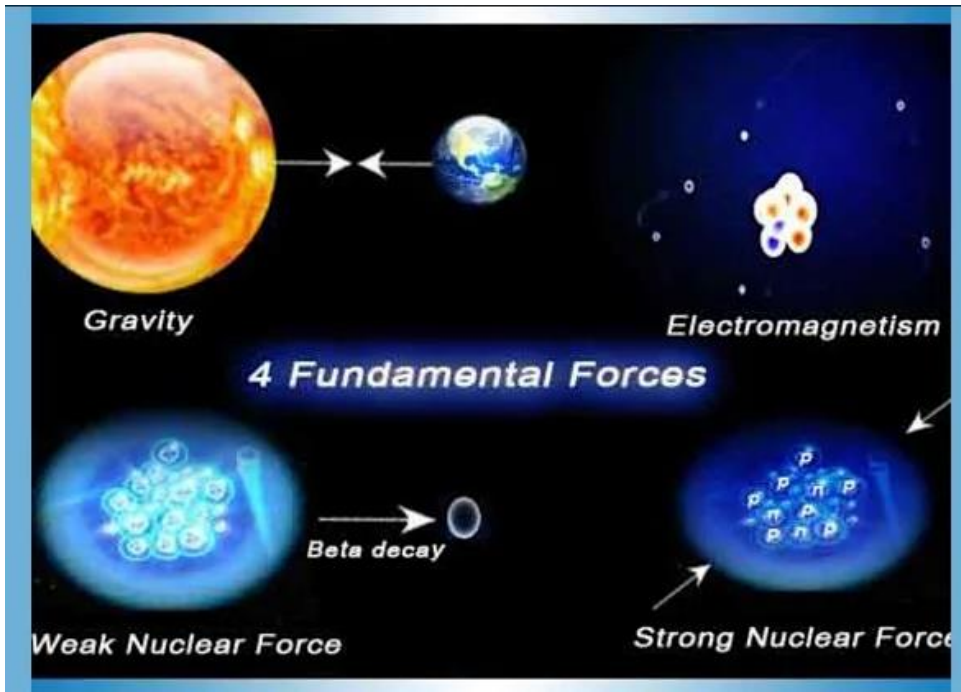
# There is no good quantum theory of everything

Even though the dynamics of the particles has been subjected to only four fundamental forces



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Even though the dynamics of the particles has been subjected to only four fundamental forces



## Grand Unified Theory (GUT)

Unifies only three fundamental forces (without gravitation)

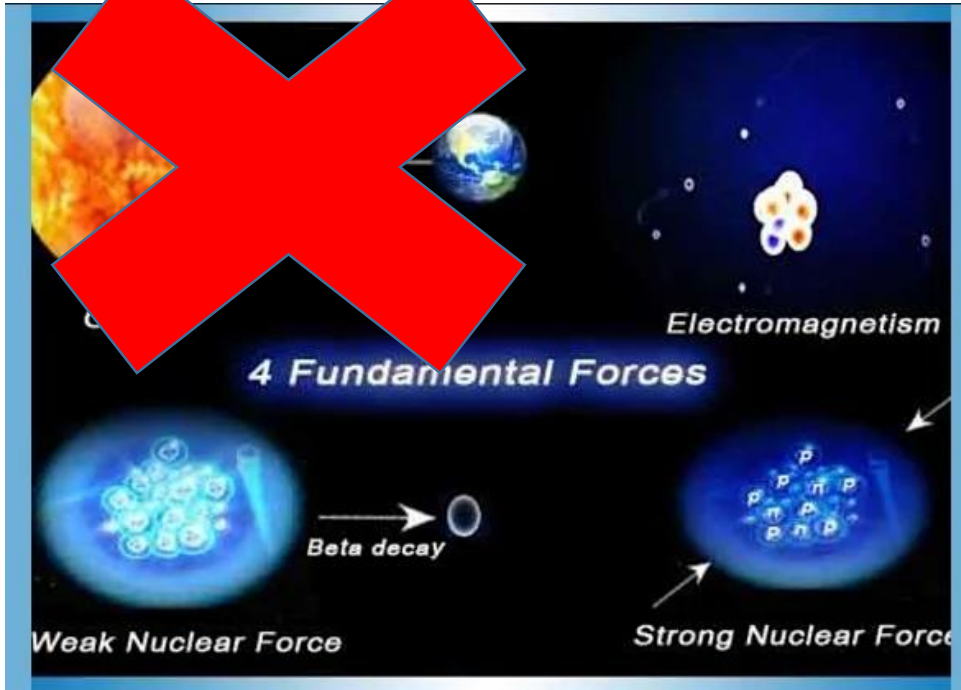
## Theory of Everything

Unifies all four fundamental forces

# There is no good quantum theory of everything

Even though the dynamics of the particles has been subjected to only **3** fundamental forces

If we forget about the gravitational force, the world is **FLAT**, described by a Quantum Field Theory

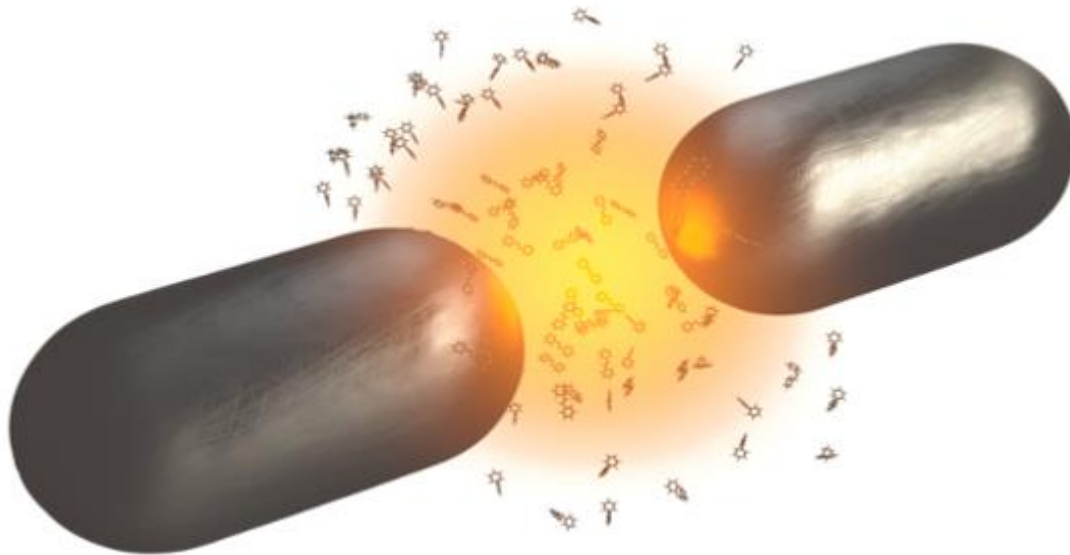


**Grand Unified Theory (GUT)**  
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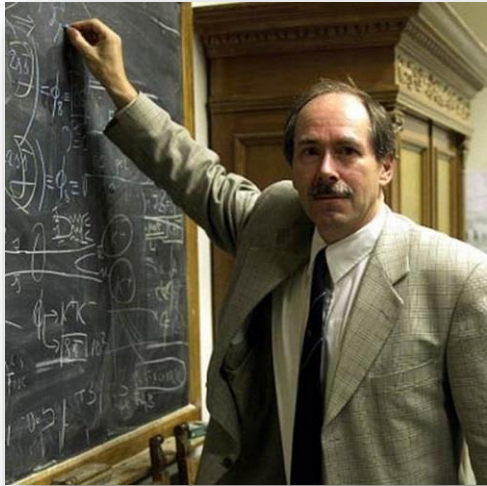
**Theory of Everything**  
Unifies all four fundamental forces

# Still there is a big problem of how to treat **the strong coupling** in the quantum field theory

Strong coupling problem appears in Condensed Matter,  
High Energy Physics, Hydrodynamics, Plasma Physics,  
Quantum Chromodynamics (QCD), Theory of Complexity,  
Information Theory, Entanglement Entropy, ...







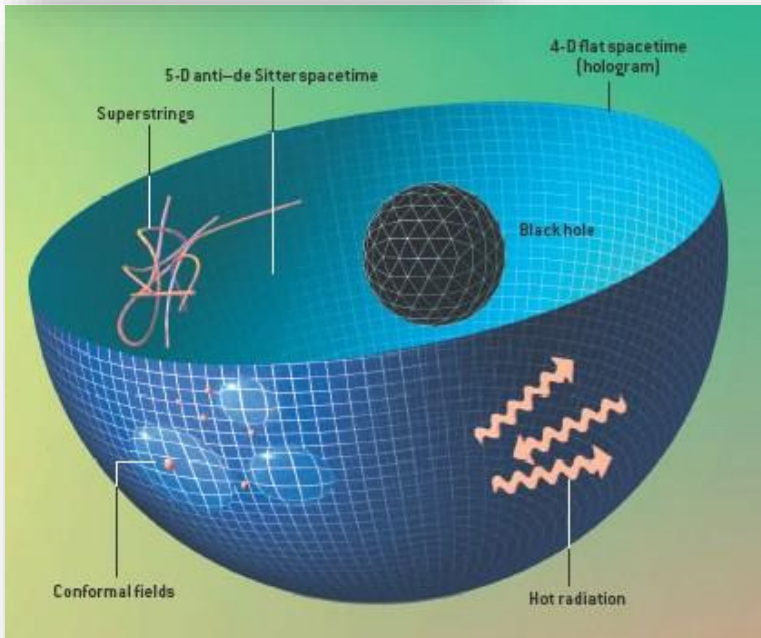
# Holographic principle

- Proposed by Gerard 't Hooft in 1993
- Developed by Leonard Susskind in 1997

## Conjecture

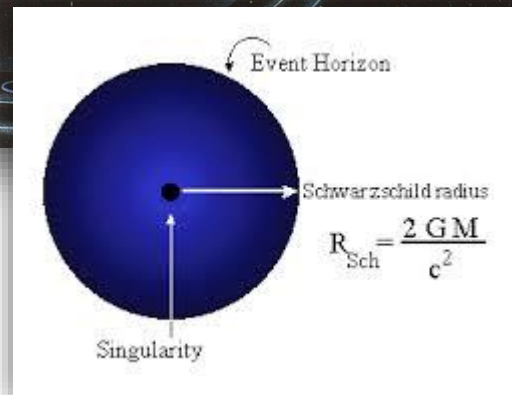
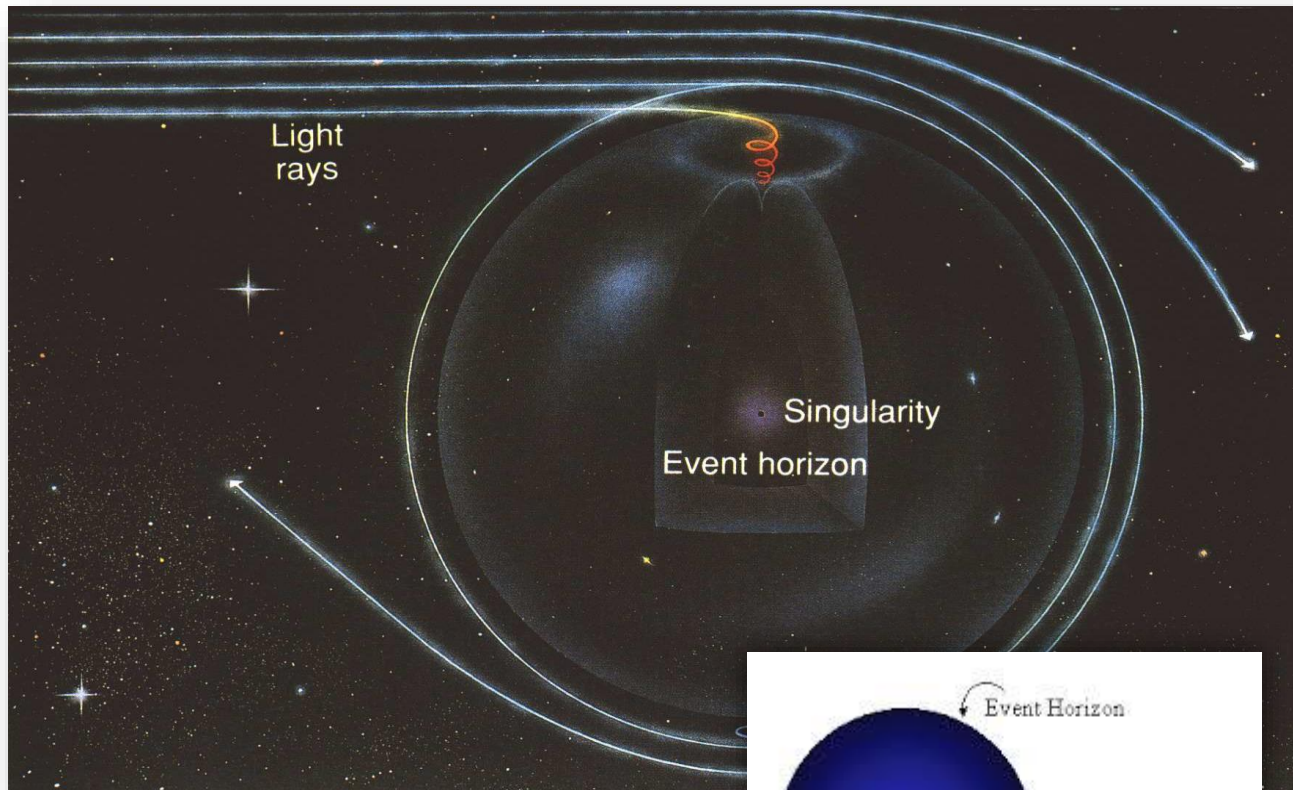
All information contained in a region of a space-time can be fully described through the degrees of freedom contained on its **boundary**. ('Holographic projection')

Interestingly, from the holographic point of view, our world is located **on the boundary**, in the **flat space**, and gravity exists only in the curved spacetime volume.



**Our real ( $d$ -dimensional) world without gravity is an effective theory which is a hologram of another world that has gravity (and it is  $d+1$  dimensional).**

# Inspiration – Black hole entropy



- **Black hole:**

A region of space-time with gravitational force so strong that nothing (not even light) can escape from it.

Black hole is enclosed in the volume within its **event horizon.**

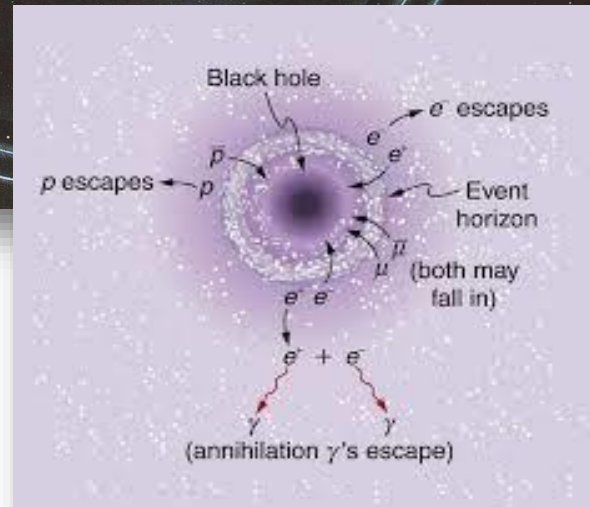
# Inspiration – Black hole entropy

Light ray

Existence of the radiation means that we can analyze **black hole thermodynamics**, its entropy and temperature.

Event horizon

Quantum effects near the horizon produce creation of particles. Some of them fall into the black hole, other not, what can be observed as **black hole radiation**.  
**(Hawking radiation)**



## • Black hole:

A region of space-time with gravitational force so strong that nothing (not even light) can escape from it.

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# Black hole thermodynamics

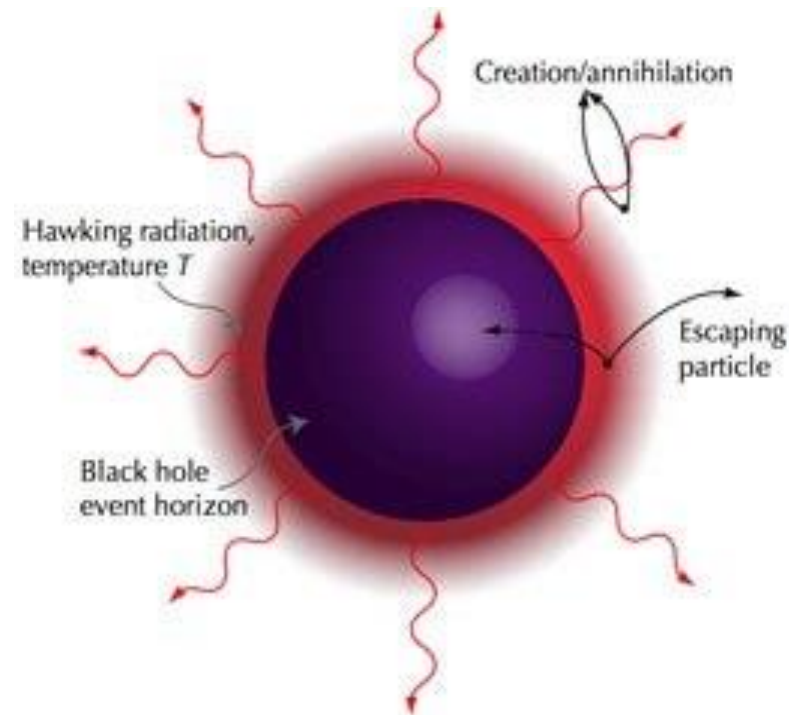
- Study of the black hole horizon from the point of view of the thermodynamic laws
- It shows the aspects of the underlying **quantum gravity**.

## Black hole radiation

### Hawking radiation

Black body radiation which is emitted by the black hole due to the quantum effects near its event horizon.

In the equilibrium, this radiation has the temperature  $T$ .





# Laws of the Black Hole thermodynamics

Equilibrium system, reversible process

## Law 0 (Concept of the temperature)

Event horizon of the stationary black hole has constant temperature.

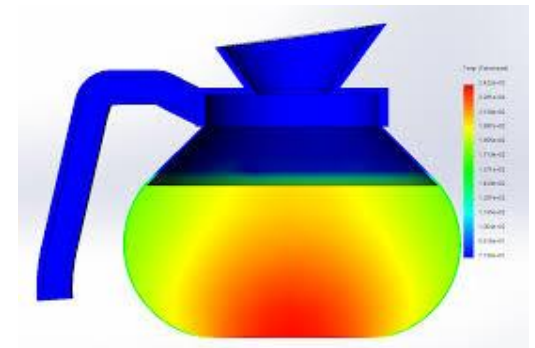
## Law 1 (Conservation of energy)

Under perturbations of a stationary black hole, the energy changes according to the conservation law:

$$\delta E = T\delta S + \Omega\delta J + \Phi\delta Q + \dots$$

**Extensive variables:**  $(E, S, J, Q, N, V, \dots)$  *global, constants*

**Intensive variables:**  $(T, \Omega, \Phi, \mu, \rho, \dots)$  *local*



# Laws of the Black Hole thermodynamics

Equilibrium system, reversible process

## Law 2 (Entropy)

The area of the horizon is a non decreasing function,  $\delta S \geq 0$ .

Bekenstein-Hawking entropy:  $S = \frac{\text{Area of the horizon}}{4}$

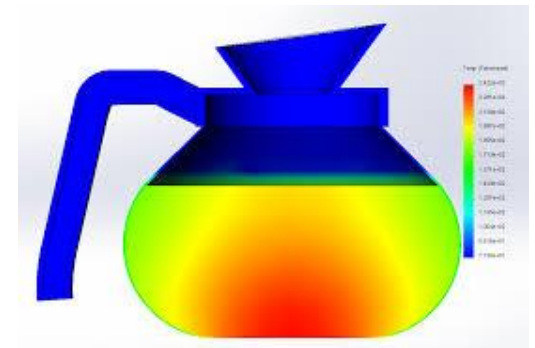
## Law 3 (Zero temperature)

Extremal black holes have zero temperature.

### Usual thermodynamic systems:

When  $T=0$ , the entropy is constant and zero.

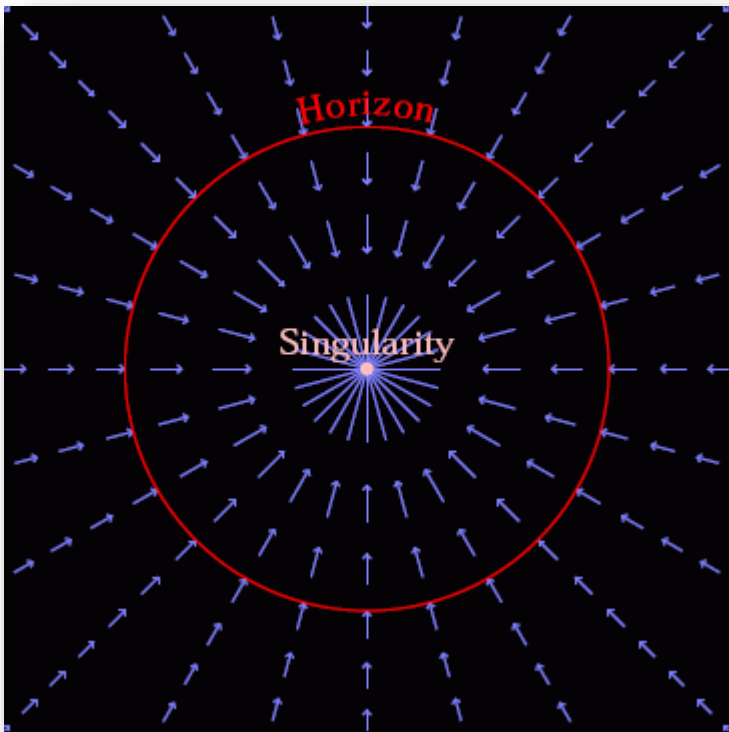
*Exceptions are non crystal solids (glass) which have constant residual entropy.*



# Holographic principle and entropy

## Example

Even horizon of the black hole

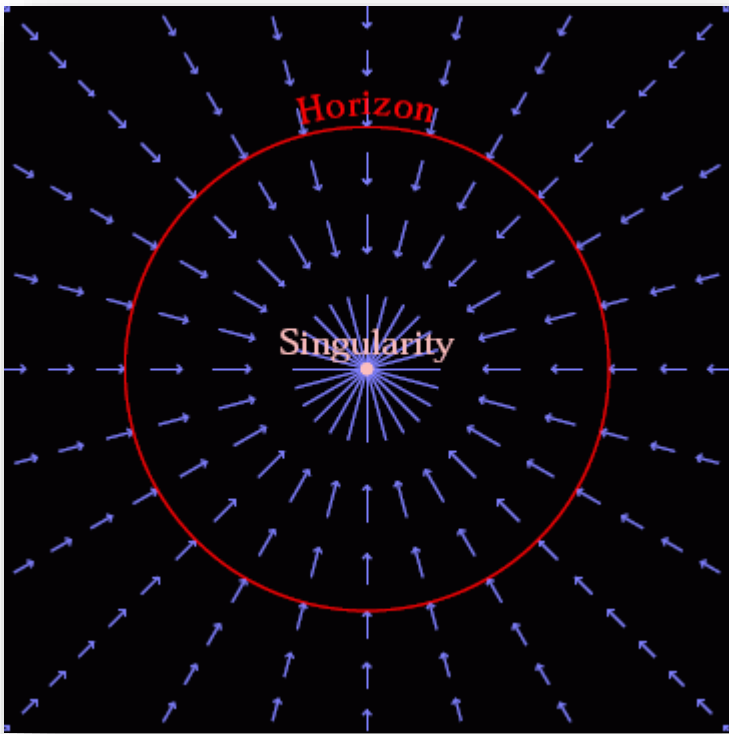


- **Our physical intuition** says that the entropy is proportional to the volume, because it is directly proportional to the mass which is proportional to the volume.
- **Thermal gas** at high  $T$  has energy and entropy
  - D=3:  $E \sim T^3, S \sim T^2$
  - D=4:  $E \sim T^4, S \sim T^3$
- 4D theory has more degrees of freedom than the 3D theory

# Holographic principle and entropy

## Example

Even horizon of the black hole

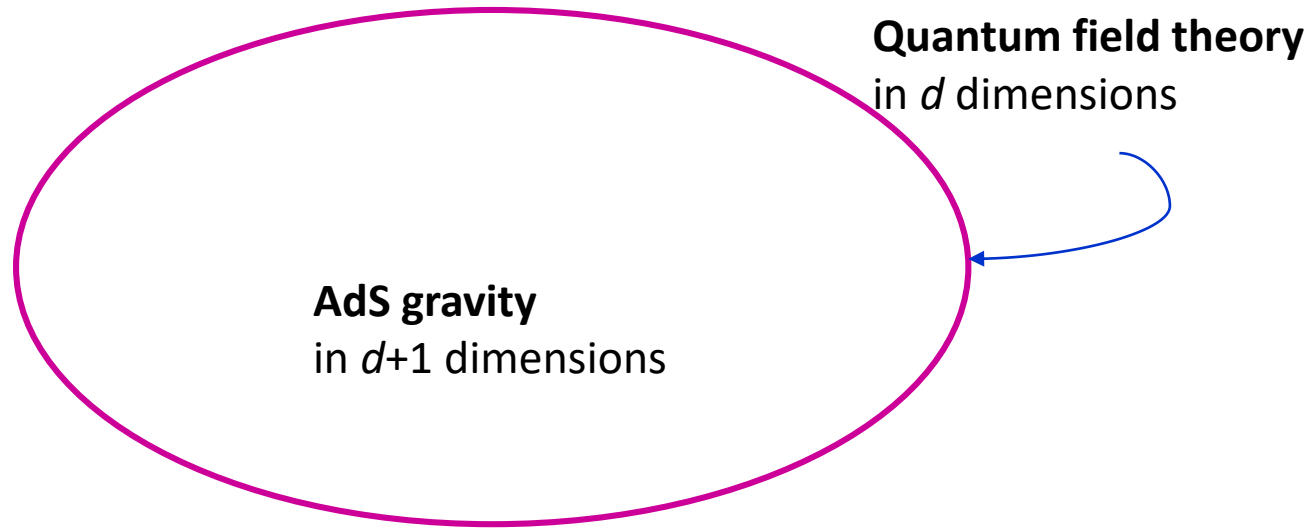


- Thermal gas at high  $T$  can collapse and form a **black hole** with the event horizon  $r_H$  and the temperature  $T \sim r_H$ .
- Energy and entropy of a black hole in 4D coincide with a thermal gas in 3D.
- This implies that the mass occupies an **area**, and not a volume, so that the whole information about the (gravitational) universe is encoded in its boundary as a **hologram**.



# AdS/CFT correspondence

This is a holographic principle applied to a  $(d+1)$ -dimensional gravity with a negative cosmological constant (i.e., **anti-de Sitter (AdS) gravity**), and a  $d$ -dimensional **conformal field theory (CFT)** living on its boundary.



# AdS/CFT correspondence

- **Conformal transformations** preserve the angles
- **Conformal symmetry** is typical in condensed matter systems close to the critical point where a phase transition occurs
- More precise mathematical statement **equals two quantum theories (AdS gravity and CFT)**, in the sense of equality of their quantum partition functions.
- In practice, we work **in classical gravity**, which corresponds to a **strongly coupled** field theory.

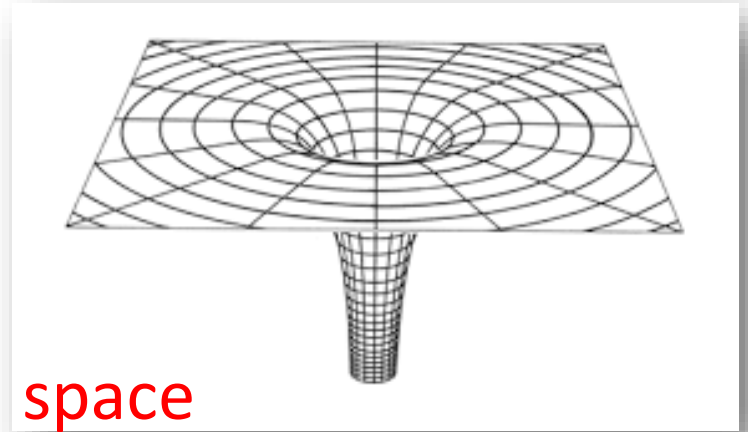


# Why AdS space?

It is a constant curvature hyperbolic space

$$-t^2 + x^2 + y^2 + z^2 - u^2 = -\ell^2$$

Its boundary is a flat (Minkowski) space



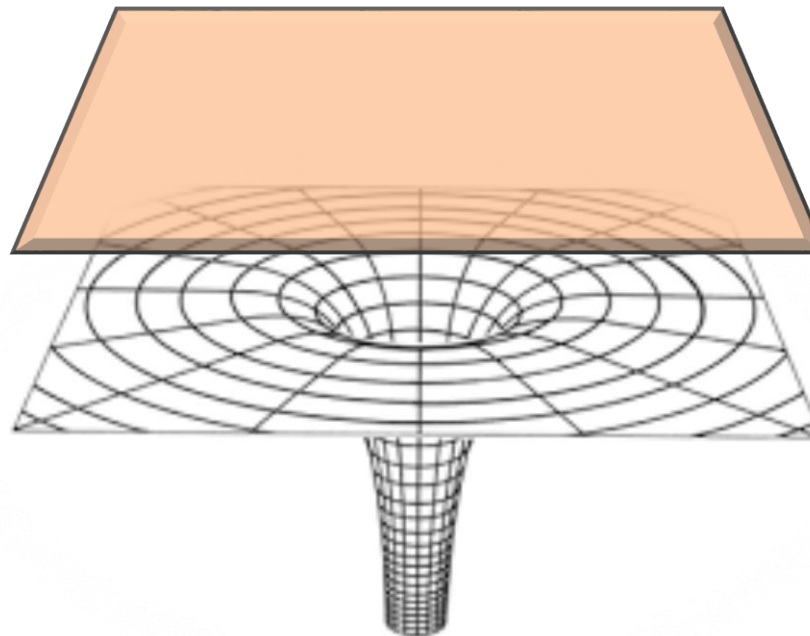
- Quantum field theory lives in the Minkowski space, which is an asymptotic boundary ( $r \rightarrow \infty$ ) of the AdS space
- Moreover, large distance in gravity corresponds to low energy in a field theory, so there is a **duality** between them
- For example, to obtain a UV finite quantum field theory (difficult), **gravity has to be IR finite (easy)**

# AdS/CFT Conjecture - summary

Classical gravity in AdS space



Conformal Field Theory on the boundary



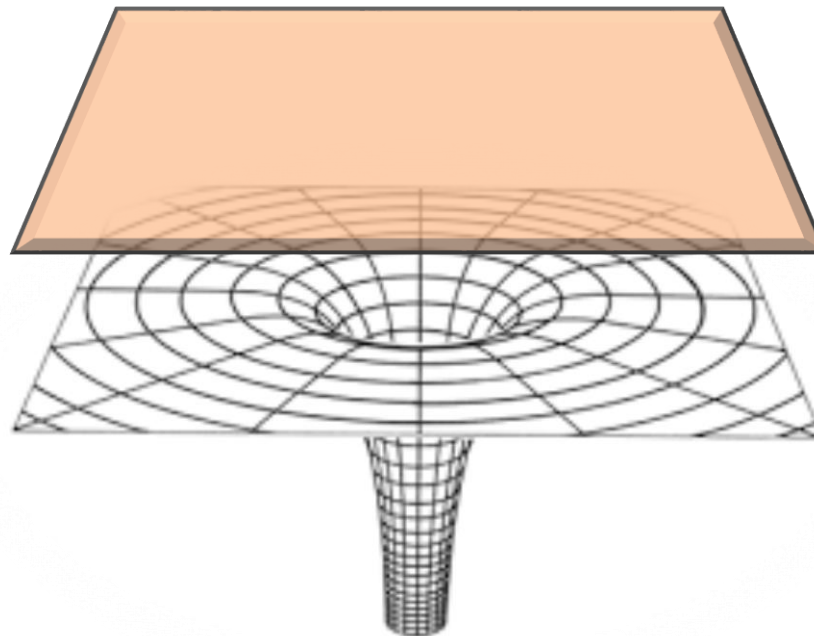
High energy

Low energy



# AdS/CFT Conjecture - summary

Holographic calculations are so important because they are a powerful **analytical mathematical tool to obtain non-perturbative results** about strongly coupled systems in the flat space .

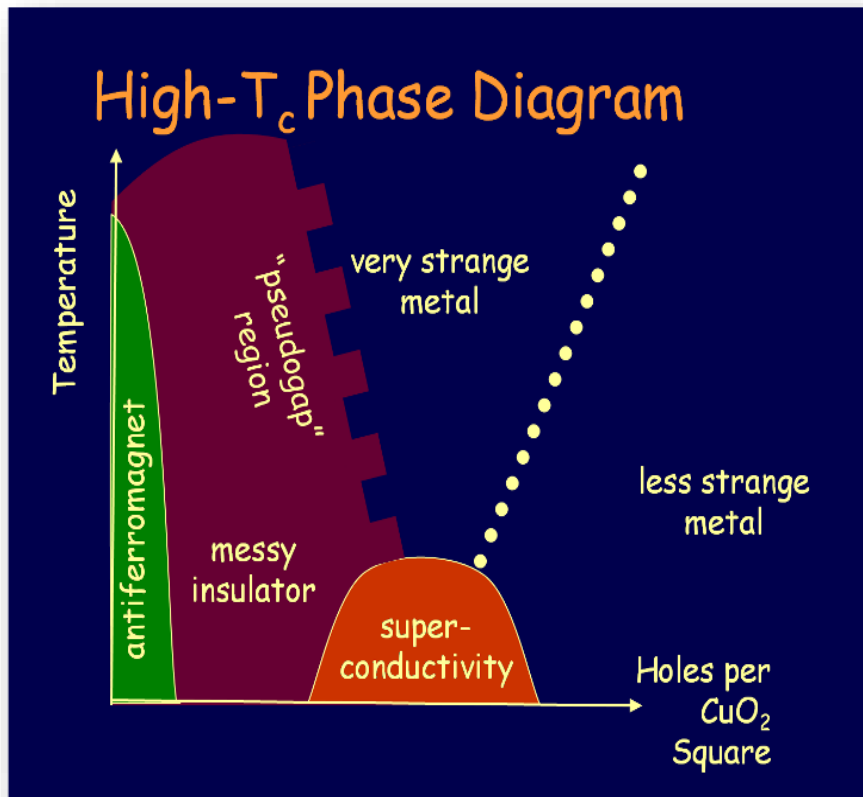


**High energy**

**Low energy**

# Application: Holographic superconductors

Properties of superconductors below some critical temperature  $T_c$

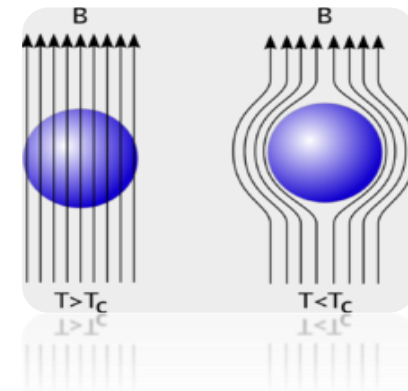


## Electric :

They conduct electric current without resistance and energy loss

## Magnetic:

Meissner effect, magnetic field cannot penetrate into the material



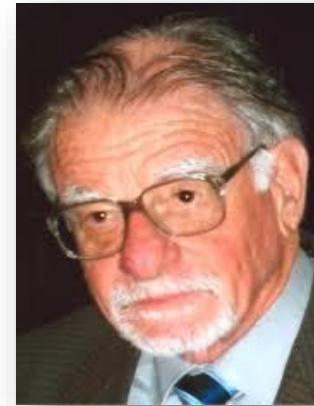
# Holographic Superconductors

## High $T_c$ superconductors

- Discovered in 1986, received Nobel Price in Physics in 1987



Johannes Georg Bednorz



Karl Alexander Müller

- There is no good microscopic theory to explain them
- BCS theory (1957) fails for  $T_c > 30\text{K}$ .

# Holographic Superconductors

**Gauge/Gravity duality** is the only analytic method to calculate properties of high  $T$  superconductors.

## How to model a physical theory of a Holographic Superconductor

Minimal field content in AdS gravity necessary to describe a superconductor in a quantum field theory

Superconductor	Gravity	Field
Has constant $T$	Has Hawking $T$ , we need a black hole	Metric, $g_{\mu\nu}(x)$
Satisfied the Ohm Law $J = \sigma E$	Charged black hole	Electromagnetic field, $A_\mu(x)$
Possess an order parameter, $O$	Hairy black hole	Scalar field, $\psi(x)$



# Holographic Superconductors

- **Superconductor is holographically dual to a hairy black hole**
- When a black hole develops hair, it corresponds to a phase transition of a superconductor from a normal state to a superconducting state



## What is black hole hair?

- **No hair theorem:** All black holes in Einstein-Maxwell gravity in asymptotically flat space in 4D can be characterized by only three classical observables from the outside:  $(M, Q, J)$ . All other information disappears on the horizon.
- **Hair** can appear in  $D > 4$ , non-flat space, no Einstein gravity, etc....

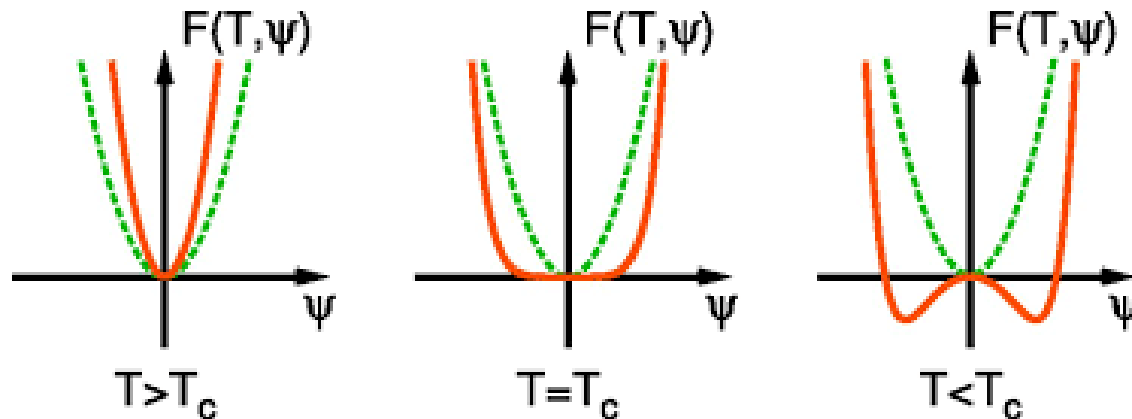
# A role of the scalar field $\psi$ (order parameter)

$\psi = 0$ , Black hole without hair,  $T \geq T_c$

Normal phase of the superconductor, free energy  $F_0$

$\psi \neq 0$ , hairy black hole,  $T \leq T_c$

Superconducting phase, free energy  $F \leq F_0$

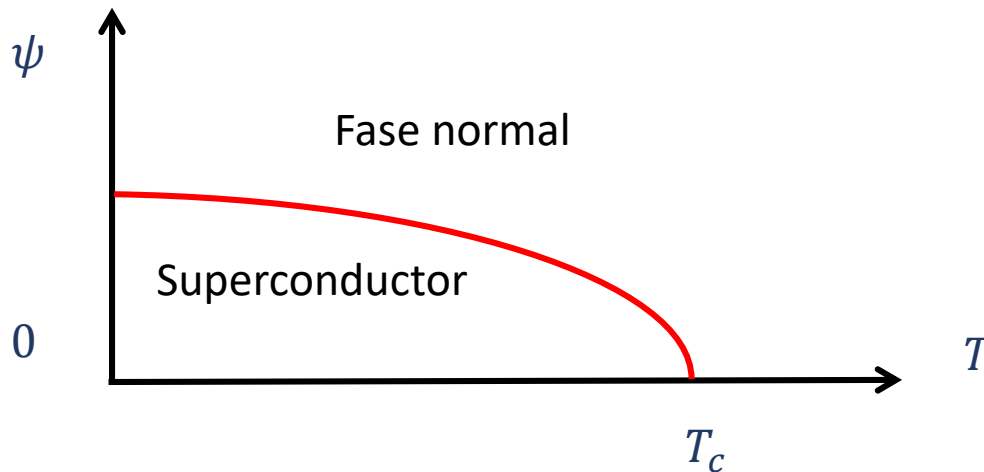


Temperature fluctuation  $T$  produces a change in the thermodynamic potential  $F$  and the scalar field  $\psi$  'detects' a change in the minimum of the potential because it acquires  $\psi \neq 0$

# A role of the scalar field $\psi$ (order parameter)

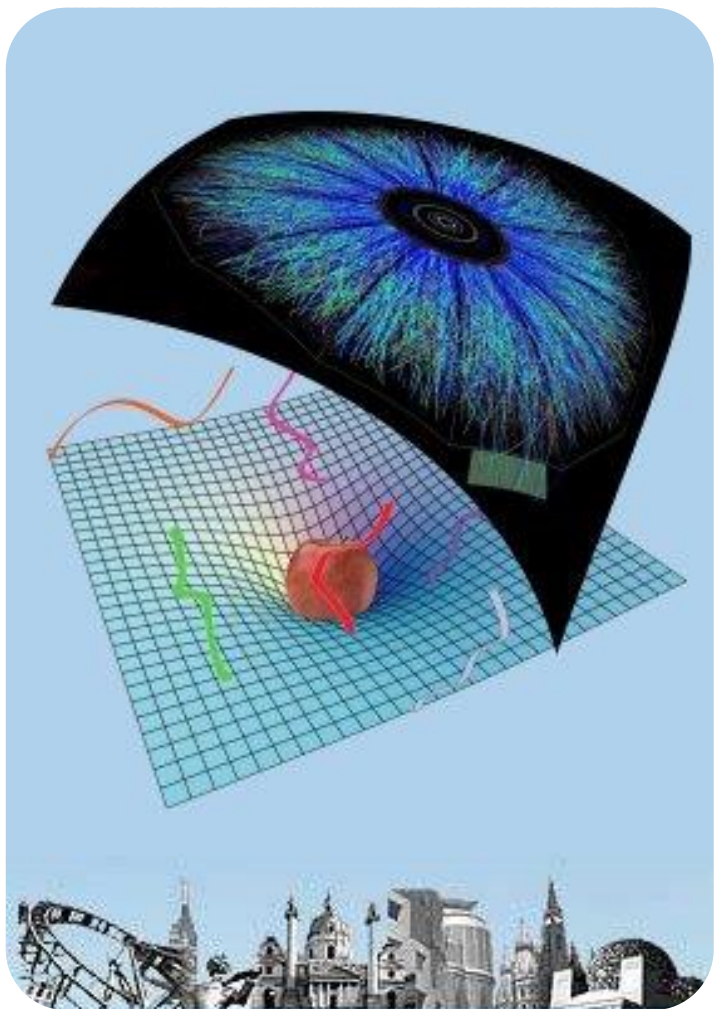
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Superconducting phase, free energy  $F \leq F_0$



Typical form of the order parameter **which describes a phase transition of the second order**, where the free energy has **discontinuous second derivative in the critical point**.

# Holographic superconductor



## Goal: to have an unstable black hole

Black hole fluctuations can be rewritten as the **Ohm law**  $J_i = \sigma E_i$  where the conductivity coefficient  $\sigma$  presents a linear response of the system to the electric field.

Gravitational equations on the boundary are scale-invariant, what is typical for phase transitions.

The duality between the superconductor and AdS gravity ensures that the Einstein equation coupled to the EM field and a scalar field contains all the **quantum information about the superconductor!**

# Holographic superconductors

## First results

*2008—2010, Franco, Hartnoll, Herzog, Gubser, Garcia-Garcia, Horowitz, ...*

- **Free energy** of the superconductor
- Coefficient – **conductivity** (inverse resistance)
- **Critical exponent** ( $\beta=1/2$ ), describes  $\psi \propto |T_C - T|^\beta$
- **Order of the phase transition**
- **Energy gap** and **energy pseudo-gap**
- Specific heat
- Meissner effect (magnetic field)

Etc.



# Holographic superconductors

## Some of our contributions to the subject

2018, JHEP, Marrani, OM, Quezada León, Case  $T=0$

2017, PRD, Cvetkovic, OM, Simic, Theories Lovelock-Chern-Simons

2017, PRD; 2016 PRD, Aranguiz, Kuang, OM , Phase transitions of black holes

2016, PRD, Araneda, Aros, OM, Olea , Duality of the Weyl tensor, Magnetic mass in gravity

....

2013, JHEP, Blagojevic, Cvetkovic, OM, Olea , Holography with torsion

...

2009, PRD, OM, Olea; 2007, JHEP, OM, Olea , IR renormalization of AdS gravity

...

2006 JHEP, Bañados, OM, Theisen , Holography in first order formalism

# Challenge: $T=0$ case

Geometry of the extremal black hole,  $T = 0$ , cannot be obtained in a continuous way from the non-extreme black hole with  $T \neq 0$  by taking  $T \rightarrow 0$ .

There is no much information about its holography in the literature



## Properties of the extremal black hole

- It has at least two event horizons that coincide
- It has minimal mass
- Does not radiate ( $T=0$ )
- It is the most stable in the family  $(M, Q, J)$
- Its entropy is not zero
- It is stable in supergravity (BPS state)
- All discovered black holes are near-extremal with  $M=J$  y  $Q=0$
- **Method of Euclidean action to find free energy fails**

# Other applications of Gauge/Gravity Duality

- Holographic hydrodynamics
- Quantum anomalies
- Non relativistic field theories
- Anisotropic field theories
- Condensed matter applications
- QCD applications
- Entanglement entropy

...



**Thank you for your attention!**



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